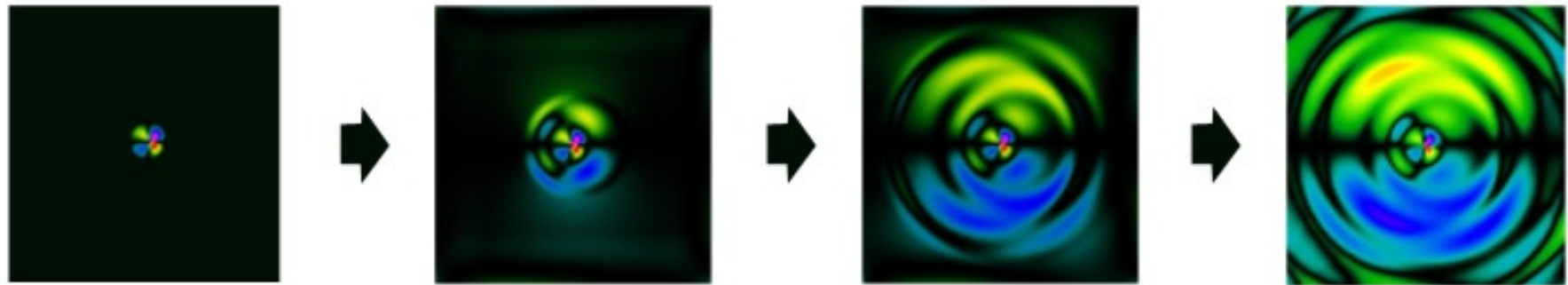


Constraints on cosmic strings from pulsar timing arrays (PTAs)



Richard Battye
Jodrell Bank Centre for Astrophysics
University of Manchester

in collaboration with Sotoris Sanidas & Ben Stappers

Constraints on cosmic strings -philosophy

- There is significant uncertainty: due to lack of detailed understanding of string networks
 - observers/experimentalists are conservative
 - they don't like theories that moving targets
- CMB: sensitive mainly to string density
 - Talk by Adam Moss -> factor of 2-3 discrepancy
- PGW : sensitive to many more things
 - loop distribution
 - radiation mechanism
- Modelling v simulations – a quagmire !
- Our philosophy is to be conservative

**POTENTIALLY MUCH
STRONGER ! BUT ...**

Present & future constraints on primordial gravitational waves

$$\Omega_{\text{gw}} = \frac{1}{\rho_{\text{crit}}} \frac{d\rho_{\text{gw}}}{d(\ln f)} \longleftrightarrow h_{\text{gw}}(f) = 1.3 \times 10^{-9} \sqrt{\Omega_{\text{gw}}(f) h^2} \left(\frac{1 \text{ nHz}}{f} \right)$$

GW energy density
per log frequency

Strain or amplitude of metric perturbation

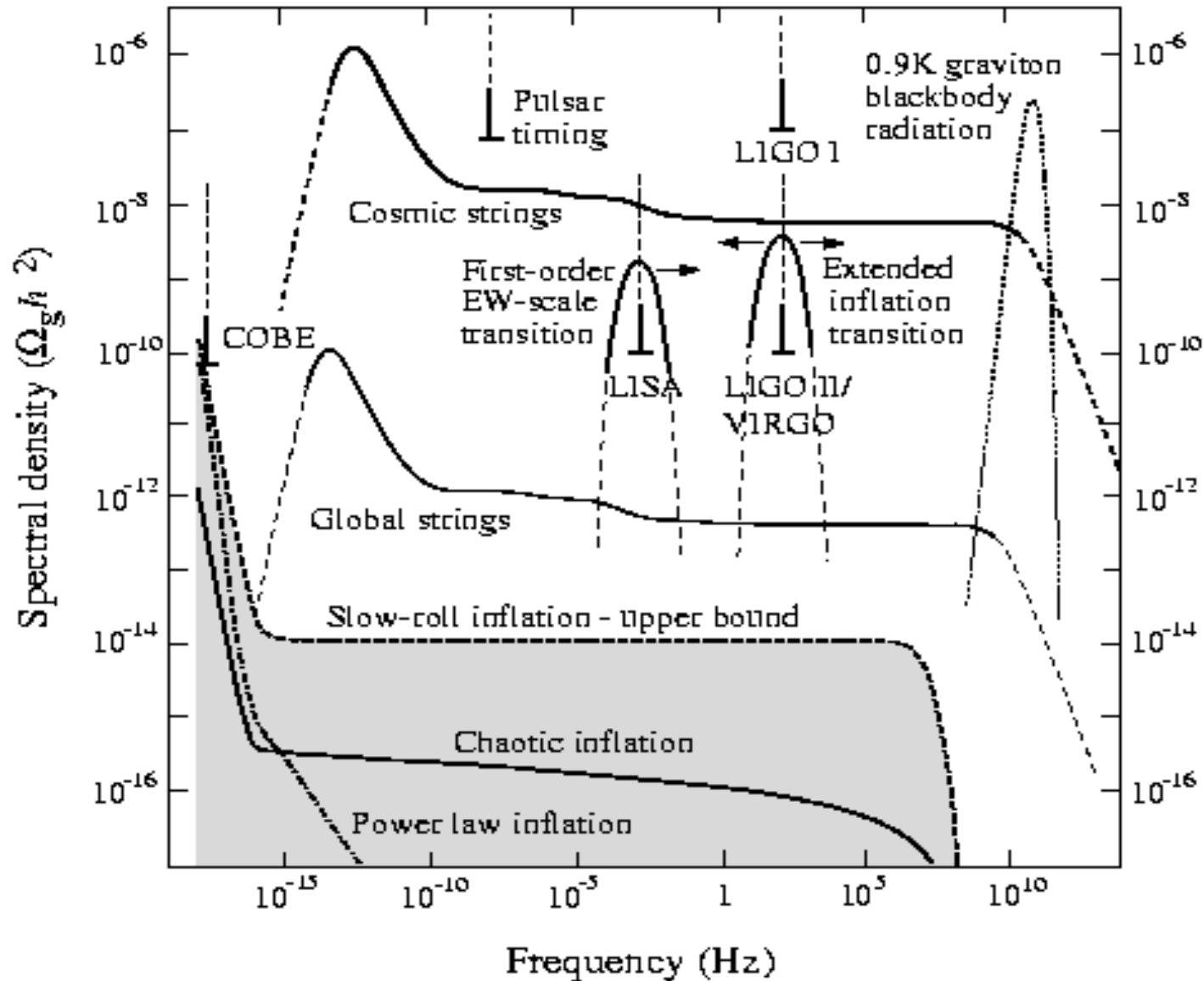
Jenet et al 2006 : $\Omega_{\text{gw}} h^2 < 2 \times 10^{-8}$

Van Haasteren et al 2011- EPTA : $\Omega_{\text{gw}} h^2 < 5.6 \times 10^{-9}$

LEAP, NanoGRAV, IPTA – improvements expected : $\Omega_{\text{gw}} h^2 \sim 10^{-10}$

SKA : $\Omega_{\text{gw}} h^2 \sim 10^{-12}$

Sources of Primordial Gravitational Waves



(BATTYE & SHELLARD 1997)

Modelling the string network

- Network parameters

- ξ = correlation length / t
- β = string wiggleness = μ_{eff} / μ
- v = r.m.s. velocity
- p = intercommutation probability)

Scaling balance
defines the amount
of energy lost by the
network

Change from radiation to matter era

- Loop distribution : a number of options

- Single loop production size = αt
- (Log-normal distribution)
- Two sizes = $\alpha_1 t$ and $\alpha_2 t$

Loop distribution defines
the spectral shape

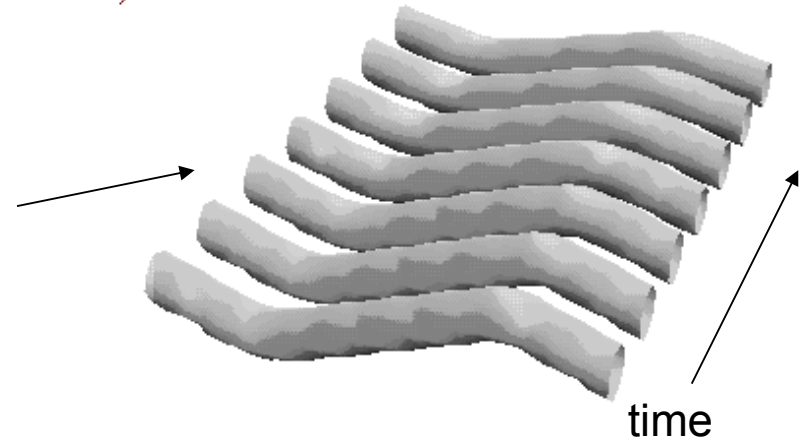
Goldstone Boson Radiation

(BATTYE & SHELLARD 1994)

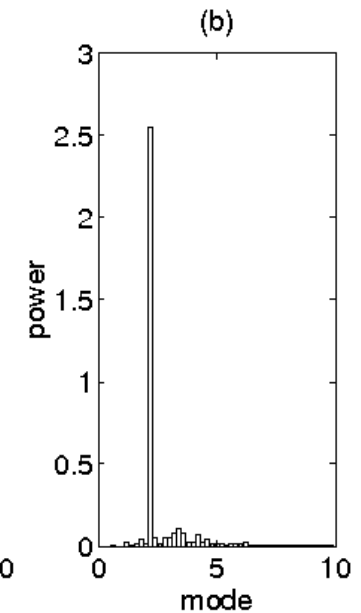
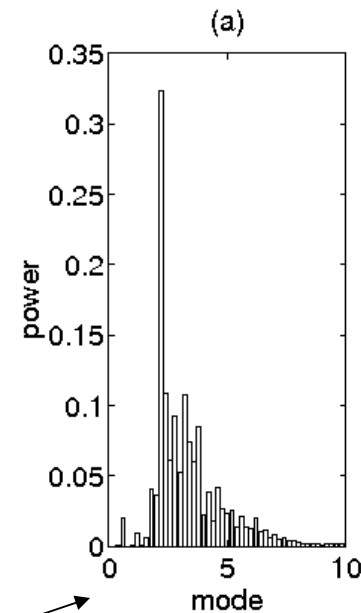
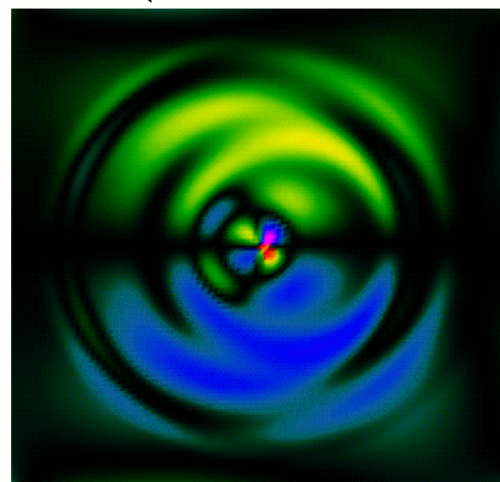
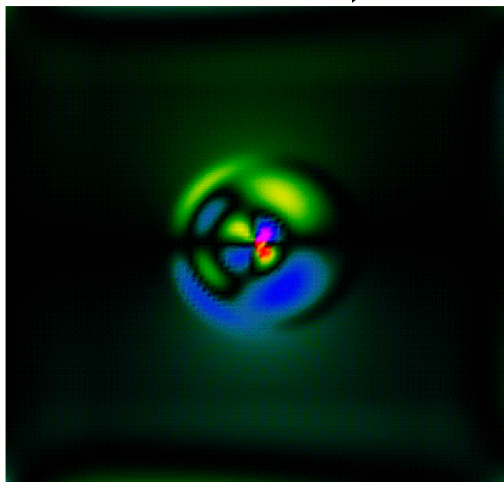
Lagrangian : $\mathcal{L} = |\partial_\mu \Phi|^2 - \frac{\lambda}{4} (|\Phi|^2 - \eta^2)^2$

where $\Phi = \phi \exp[i\theta]$

Energy density
isosurfaces for a
straight string



Goldstone boson radiation



Spectrum of radiation, P_n

Gravitational Radiation

Very similar to Goldstone boson radiation!

eg. $P \propto (\hat{J}^{\mu\nu})^* \hat{J}_{\mu\nu}$ - GB radiation

$$P \propto (\hat{T}^{\mu\nu})^* \hat{T}_{\mu\nu} - \frac{1}{2} |\hat{T}|^2 \quad \text{- Grav radiation}$$

Power : $P = \sum_{n=1}^{\infty} P_n = \Gamma G \mu^2 c$

where $P_n \propto n^{-q}$ $\Gamma \sim 50$

$q = 4/3$ - cusps & $q = 5/3-2$ - kinks

Timescale for loop decay: $\frac{t_d}{t_b} \sim \frac{\alpha}{\Gamma G \mu}$

Spectrum of Radiation

Nambu EOM: $\ddot{X} - X'' = 0$ $\dot{X}^2 + X'^2 = 1$ $\dot{X} \cdot X' = 0$

$\longrightarrow X = \frac{1}{2}(a(\zeta - t) + b(\zeta + t))$ $\longrightarrow a'^2 = 1$ $b'^2 = 1$

\longrightarrow Evolution leads to cusps $P_n \propto n^{-4/3}$

Open question: what are the effects of backreaction

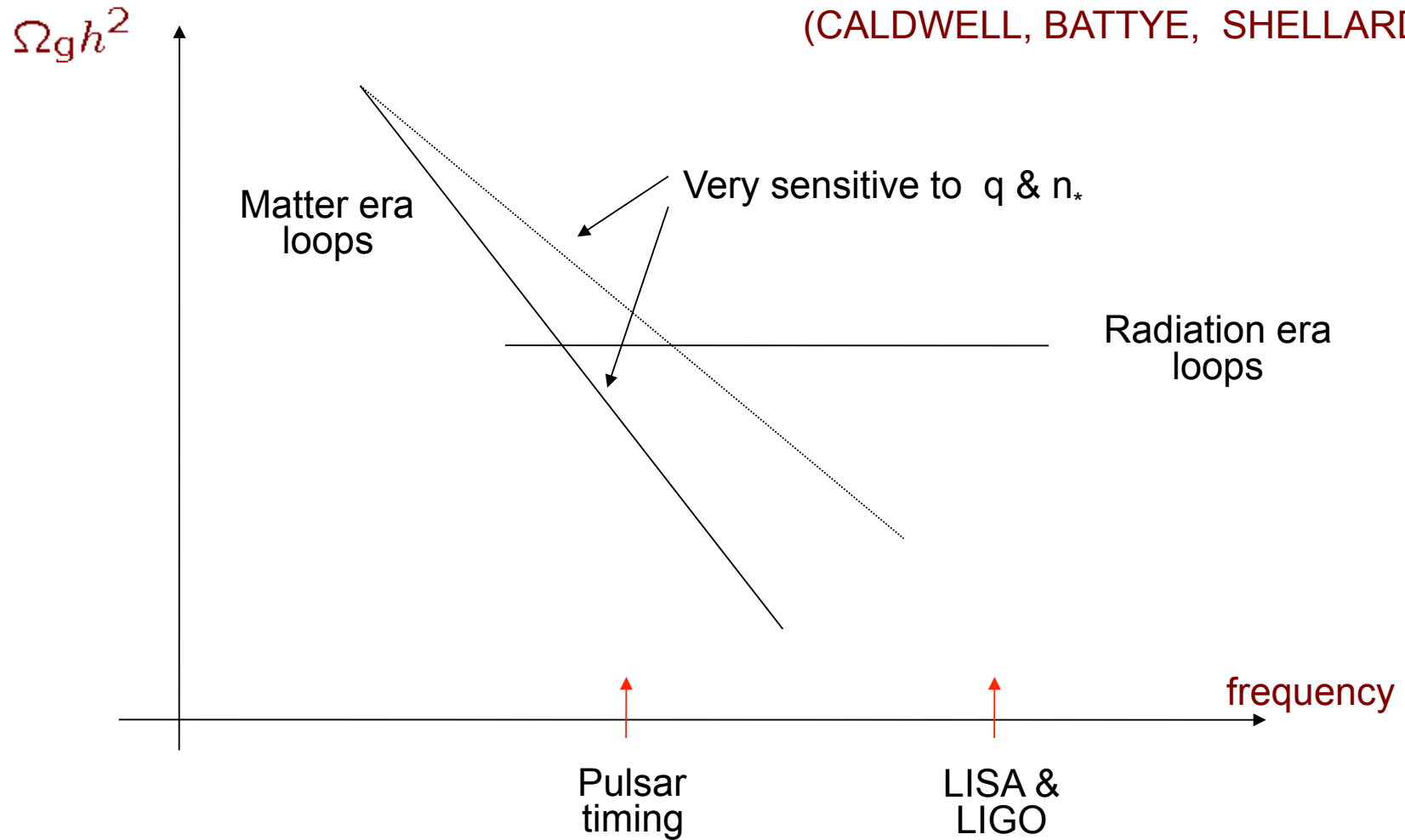
EOM becomes- $\mu(\Delta) (\ddot{X} - X'') = F^{\text{rad}}$

Assertion, either :

(i) $P = \sum_{n=1}^{n_*} P_n$ where $n_* \ll \frac{L}{\delta}$ (ii) $q > 2$

Cosmic string spectrum

(CALDWELL, BATTYE, SHELLARD 1996)



Parameters : $\alpha, \Gamma, G\mu, \xi, q, n_*$ where $P \propto \sum_{n=1}^{n_*} n^{-q}$

Conservative estimate

BATTYE, GARBRECHT
& MOSS (2006)

- Radiation era spectrum can be computed

$$\Omega_{\text{g}} h^2 = 4.7 \times 10^{-4} \frac{G\mu}{c^2} \left(\frac{1 - \langle v^2 \rangle}{\xi_{\text{rad}}^2 \Omega_{\text{m}}} \right) \frac{(1 + 1.4x)^{3/2} - 1}{x}$$

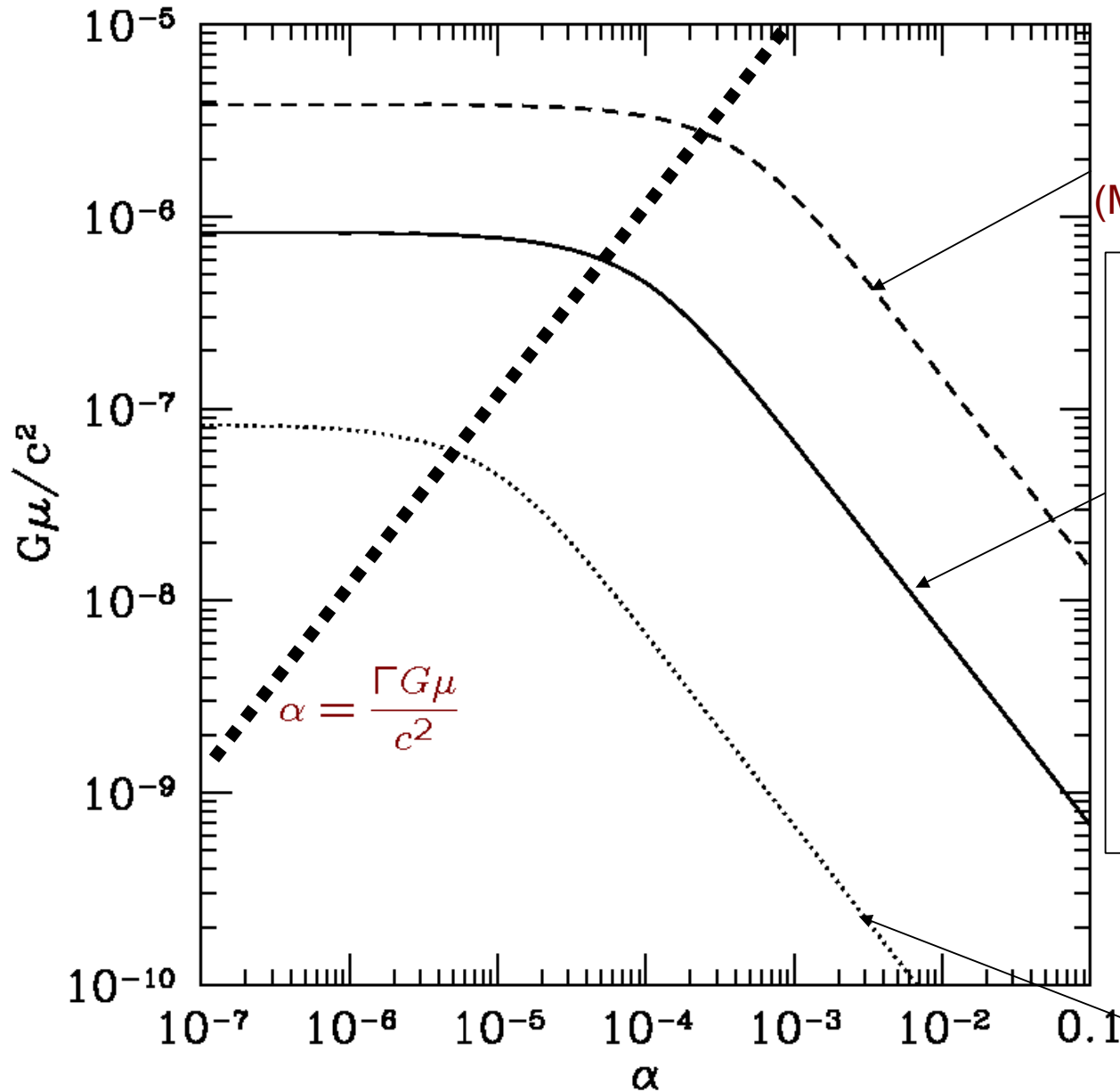
where $x = \frac{\alpha c^2}{\Gamma G\mu}$

- this is a lower bound of the signal
- use this to establish a conservative upper bound
- need measured values for

$$\xi_{\text{rad}}, \langle v_{\text{rad}}^2 \rangle, \Omega_{\text{m}}$$

Conservative constraint of string tension

BATTYE, GARBRECHT & MOSS (2006)



$\Omega_{gh^2} < 10^{-7}$
(McHUGH ET AL 1996)

(JENET ET AL 2006)
 $\Omega_{gh^2} < 2 \times 10^{-8}$

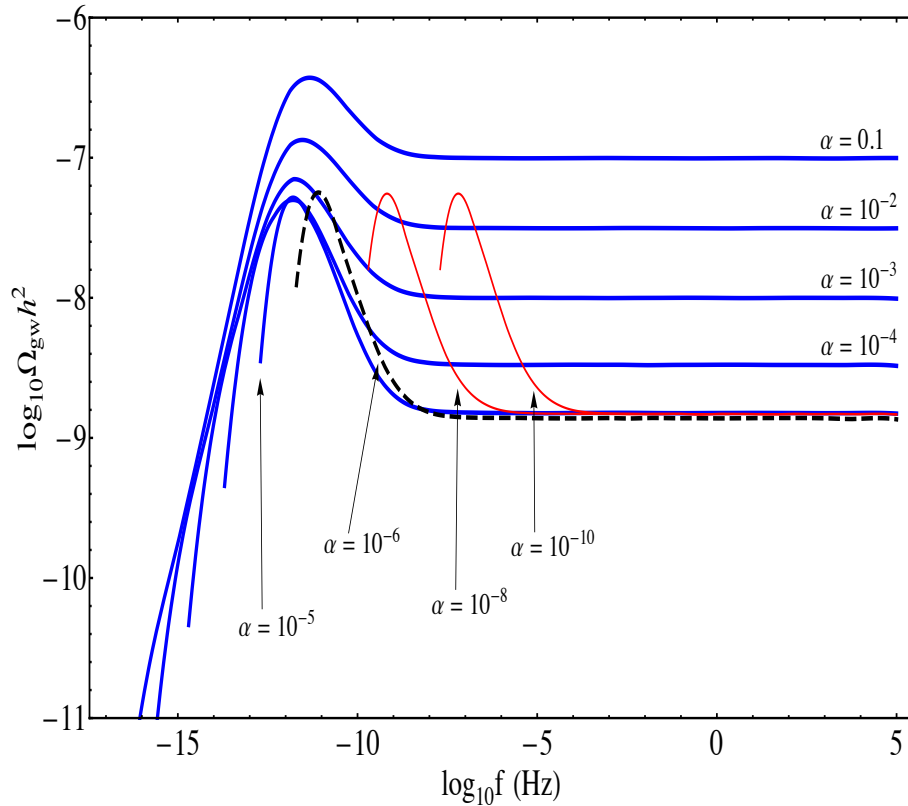
↓

$\frac{G\mu}{c^2} < 8 \times 10^{-7}$	$\frac{\alpha}{\Gamma G\mu} \ll 1$
$\frac{G\mu}{c^2} < \frac{10^{-10}}{\alpha}$	$\frac{\alpha}{\Gamma G\mu} \gg 1$

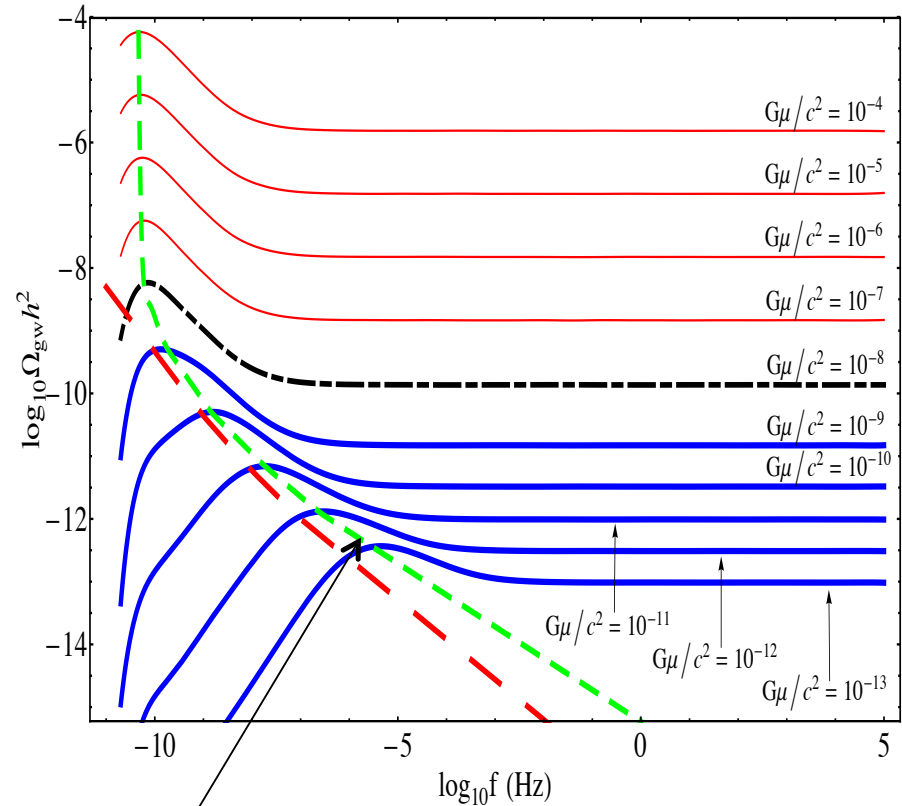
(Discredited !)

$\Omega_{gh^2} < 2 \times 10^{-9}$
(VAN LOMMEN ET AL 2002)

Cosmic string spectra : 1



Varying α for fixed $G\mu/c^2$

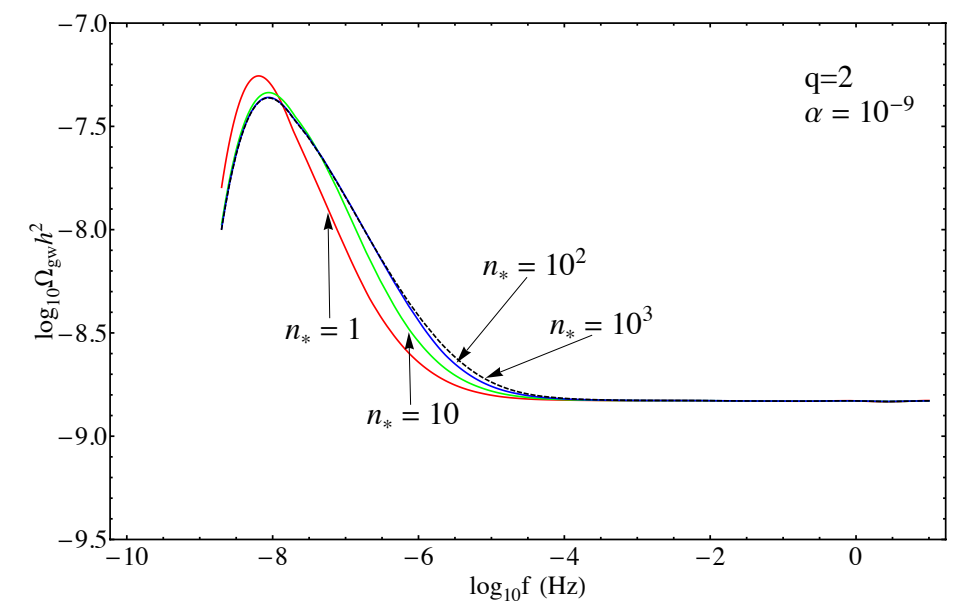
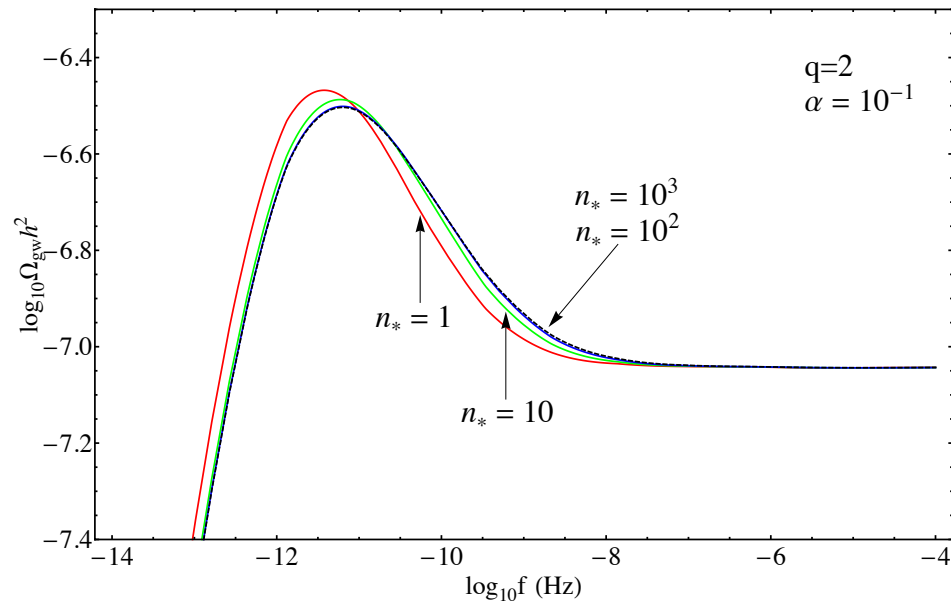
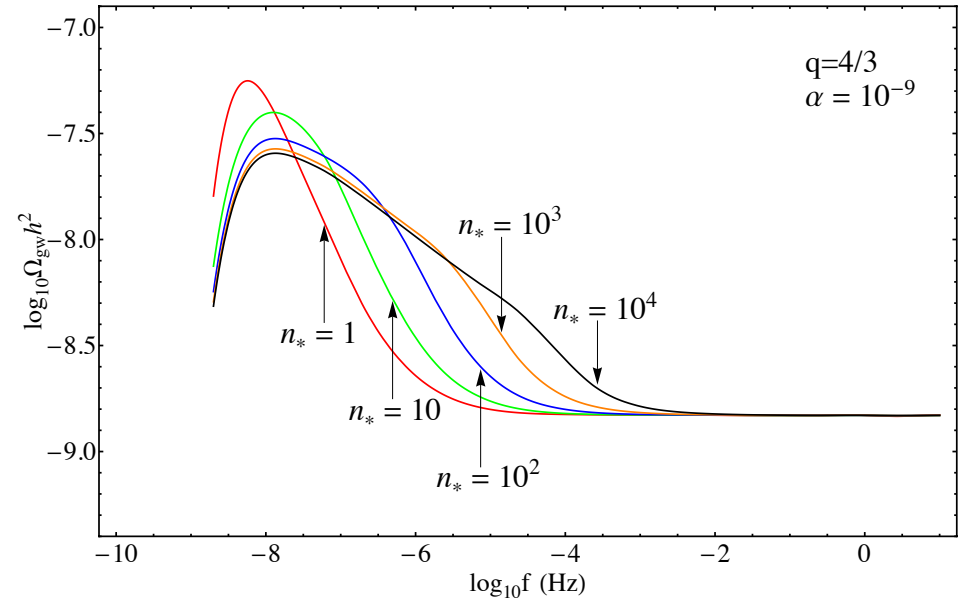
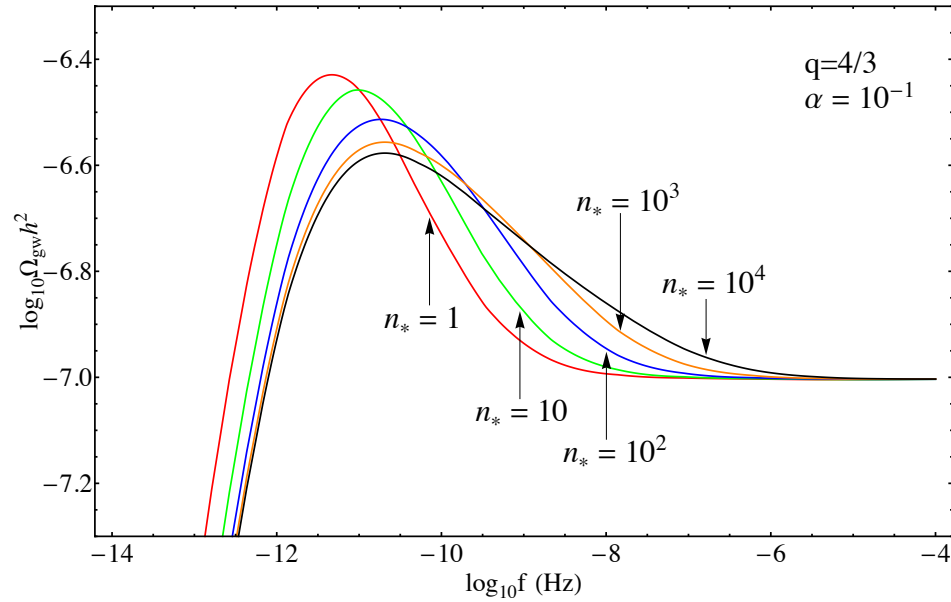


Varying $G\mu/c^2$ for fixed α

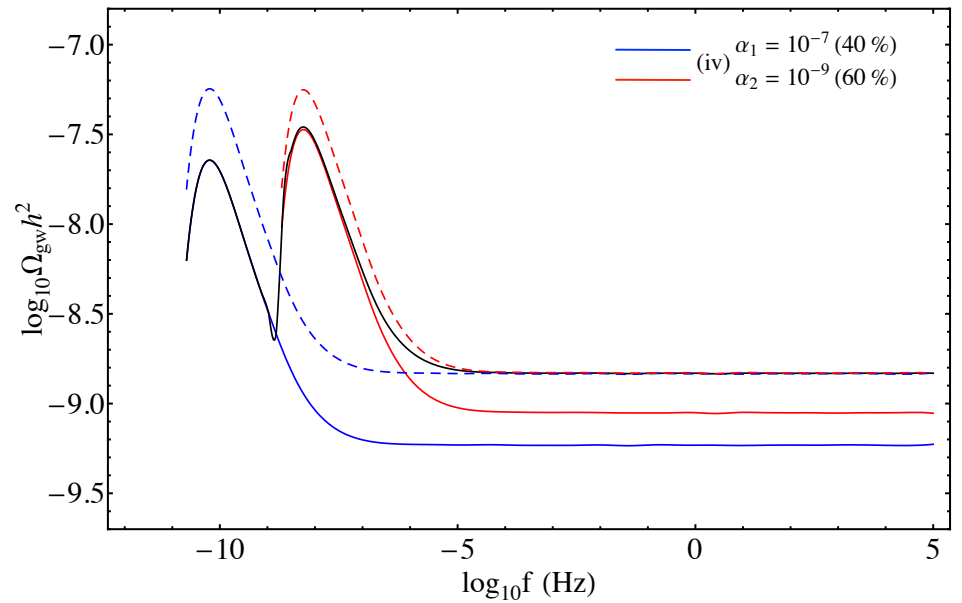
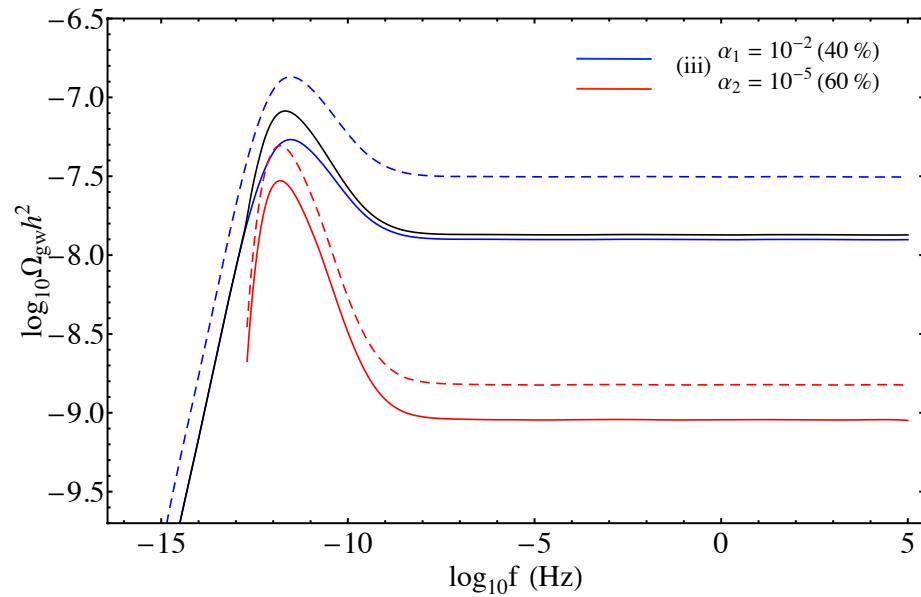
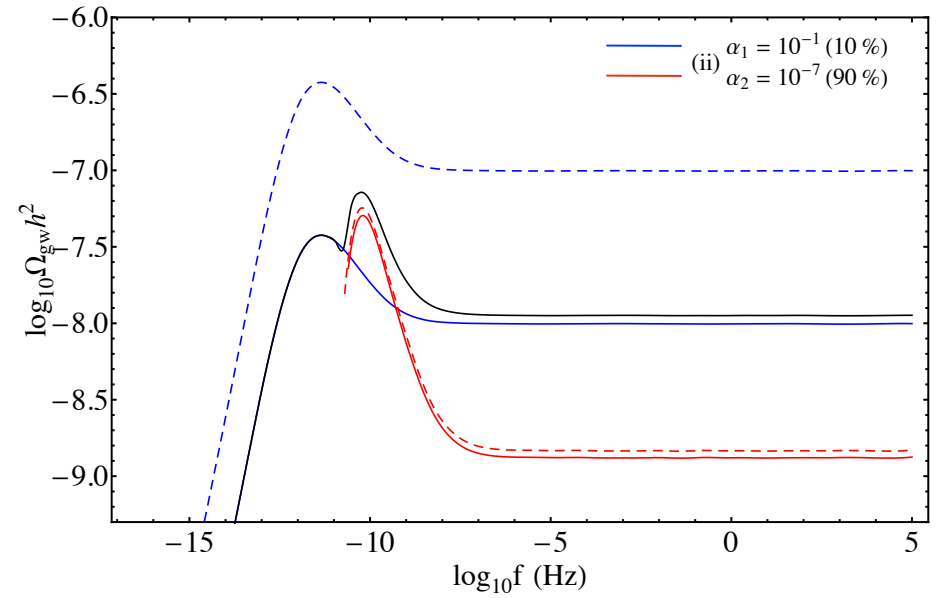
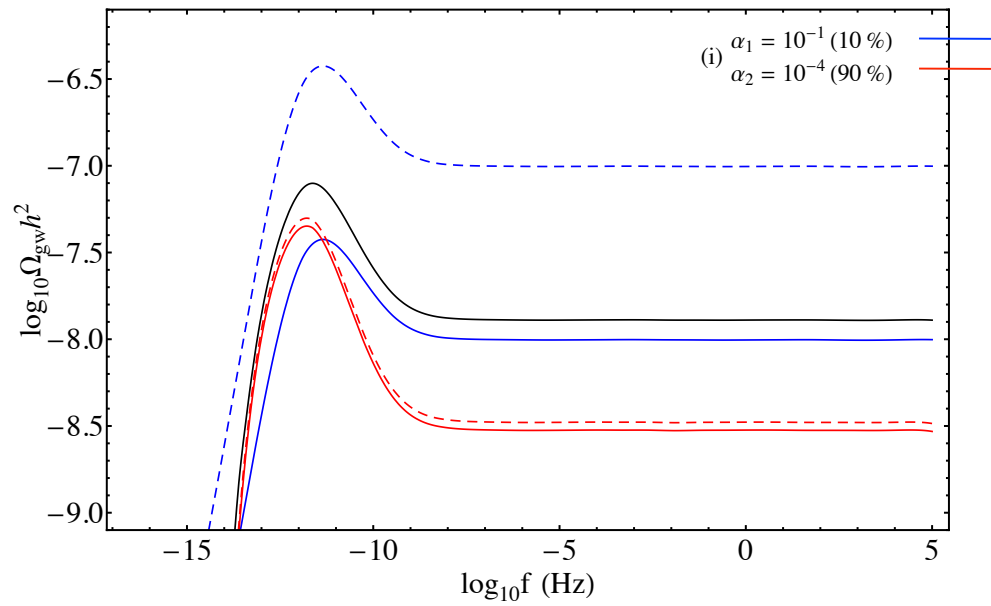
Dashed line is $\alpha = \Gamma G\mu/c^2$

Analytic approximation to frequency of maximum signal

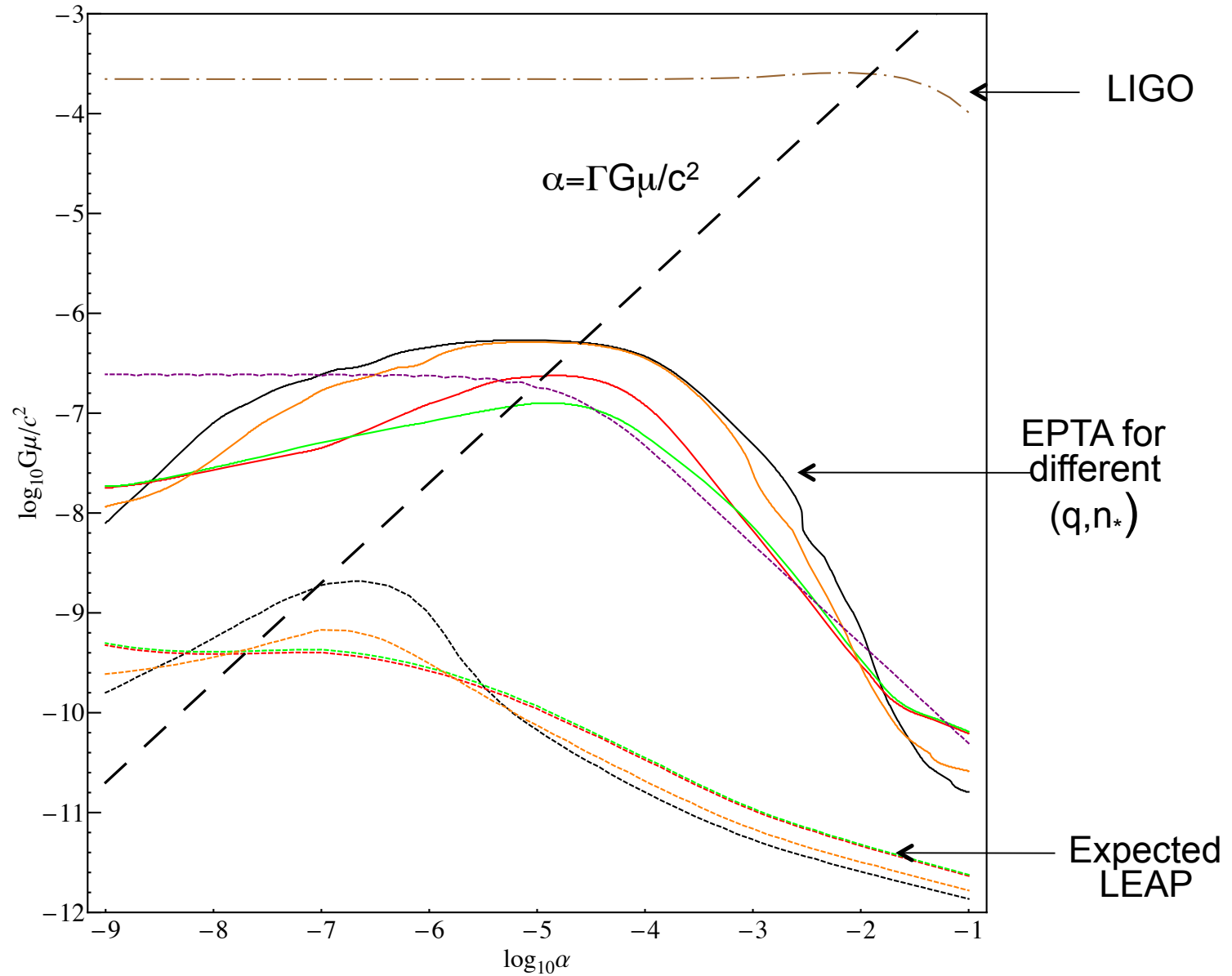
Cosmic string spectra : 2



Cosmic string spectra : 3



Present ultra-conservative limits



Specific choices of loop production size

<u>α</u>	NB Blanco-Pilado, Olum & Shlaer $< 2,8 \times 10^{-9}$	<u>$G\mu/c^2$ bound</u>
0.1		6.5×10^{-11}
0.05		8.8×10^{-11}
0.01		7.0×10^{-10}
$\Gamma G\mu/c^2$		5.3×10^{-7}
10% 0.1 & 90% $\Gamma G\mu/c^2$		4.1×10^{-8}
10^{-9}		1.9×10^{-8}

Most conservative is 5.3×10^{-7} when $\alpha = \Gamma G\mu/c^2$

(Using limits from the European Pulsar Timing Array – EPTA)

Future limits

